

## **M.A./ M.Sc. MATHEMATICS**

### **NOTICE**

1. The Ordinances Governing the examination in the Faculties of Arts, Fine Arts, Social Sciences, Science, Commerce, Management, Engineering, Education and Law are contained in separate booklet. The students are advised to refer to the same.
2. Changes in Statutes/ Ordinances/ Rules/ Regulations/ Syllabus and Books may, from time to time, be made by amendment or remaking , and a candidate shall, except in so far as the University determines otherwise comply with any change that applies to years he has not completed at the time of change.

**Note :** The decision taken by the Academic Council shall be final.

## **M.A./ M.Sc. MATHEMATICS SCHEME OF EXAMINATION - 2013**

Each Theory Paper 3 Hrs. duration

100 Marks

Dissertation/ Thesis/Survey Report/ Fixed work. if any 100 Marks

1. The number of paper and the maximum marks for each paper practical shall be shown in the syllabus for the subject concerned. It will be necessary for a candidate to pass in the theory part as well as in the practical part (Wherever prescribed) of a subject/ Paper separately.
2. A candidate for a pass at each of the Previous and the Final Examination shall be required to obtain (i) atleast 36% marks in the aggregate of all the paper prescribed for the examination and (ii) atleast 36% marks in practical (s) wherever prescribed at the examination, provided that if a candidate fails to secure atleast 25% marks in each individual paper work, wherever prescribed. He shall be deemed to have failed at the examination not with standing his having obtained the minimum percentage of marks required in the aggregate for that examination. No division will be awarded at the Previous Examination,. Division shall be awarded at the end of the Final Examination on the combined marks obtained at the Previous and the Final Examination taken together, as noted below :

First Division	60%	of the aggregate marks taken togther of
Second Division	48%	the Previous and the Final Examination.

All the rest will be declared to have passed the examinations.
3. If a candidate clears any paper(s) practical(s)/ Dissertation prescribed at the Previous and /or Final Examination after a continuous period of three years, then for the purpose of working out his division the minimum pass marks only viz 25% ( 36% in the case of practical) shall be taken into account in respect of such paper (s) Practical(s) Dissertation are cleared after the expiry of the aforesaid period of three year, provided that in case where a candidate require more than 25% marks in order to reach the minimum aggregate as many marks out of those actually secured by him will be taken into account as would enable him to make the deficiency in the requisite minimum aggregate.
4. The Thesis /Dissertation/ Survey Report. Field Work shall be typed & written and submitted in triplicate so as to reach the office of the Registrar atleast 3 weeks before the commencement of the theory examinatiion. Only such candidates shall be permitted to offer dissertation/ Fields work/ Survey report. Thesis (if provided in the scheme of examination) in lieu of a paper as have secured atleast 55% marks in the aggregate of all scheme, irrespective of the number of papers in which a candidate actually appeared at the examination.

N.B.(i) Non-Collegiate candidates are not eligible to offer dissertation as per Provision of O.170-A.

## M.A. /M.Sc. (Maths) Examination-2013

There shall be 10 Papers in all out of these five shall be offered in previous and 5 in final. Each paper shall be of 100 marks and of 3 hours duration.

### M.A. / M.Sc. (Final) Examination 2013

#### Compulsory Papers

VI.	Functional Analysis	3 Hrs	100
VII.	Topology	3 Hrs	100

#### Optional Papers (Any Three)

Opt I	Operations Research	3Hrs	100
Opt II	Fluid Mechanics	3Hrs	100
Opt III	Mathematical Statistics	3 Hrs	100
Opt IV	Information Theory	3 Hrs	100
Opt V	Programming in C with ANSI Features	3 Hrs	100
Opt VI	Fundamentals of Computer Science	3 Hrs	100
Opt VII	Computer Architecture & Data Structure	3 Hrs	100
Opt VIII	Relativity	3 Hrs	100
Opt IX	Astronomy	3 Hrs	100
Opt X	Mathematical Modelling	3 Hrs	100
Opt XI	Hypergeometric Functions & Polynomials	3 Hrs	100

## **M.A. / M.Sc. ( Final )- Optional Papers**

### **Opt. Paper - I- OPERATIONS RESEARCH**

3 Hrs. duration

Max. Marks – 100

**Note :** The question paper will contain three sections as under –

**Section-A :** One compulsory question with 10 parts, having 2 parts from each unit, short answer in 20 words for each part. Total marks : 10

**Section-B :** 10 questions, 2 questions from each unit, 5 questions to be attempted, taking one from each unit, answer approximately in 250 words.

Total marks : 50

**Section-C :** 04 questions (question may have sub division) covering all units but not more than one question from each unit, descriptive type, answer in about 500 words, 2 questions to be attempted. Total marks : 40

#### **Unit - I**

Linear Programming :- Simplex methods. Theory of simplex method. Duality, Dual Simplex methods. Sensitivity analysis

#### **Unit - II**

Game Theory :- Two person Zero sum game, Games with mixed Strategies, Solution of Linear programming. Integer Programming,

#### **Unit - III**

Network Analysis :- Shortest Path Problem minimum spanning tree Problem, Maximum flow problem, minimum cost flow problem.

Dynamic Programming :- Deterministic models

#### **Unit - IV**

Inventory problems and their analytical structures. Simple deterministic problems. Sequencing  
Nonlinear Programming :- One and multivariable unconstrained Optimization, K.T. Conditions for Constrained Optimization.

#### **Unit - V**

Quadratic programming, Queuing System :- Steady state solution of queuing model, : M/M/1, M/M/1 with limited waiting space, M/M/C, M/M/C with limited waiting space.

#### **References :-**

- 1.Kanti Swaroop: Operations Research, S.Chand Publications
- 2.S.D.Sharma: Operations Research

### **Opt. Paper - II -FLUID MECHANICS**

3 Hrs. duration

Max. Marks – 100

**Note :** The question paper will contain three sections as under –

**Section-A :** One compulsory question with 10 parts, having 2 parts from each unit, short answer in 20 words for each part. Total marks : 10

**Section-B :** 10 questions, 2 questions from each unit, 5 questions to be attempted, taking one from each unit, answer approximately in 250 words.

Total marks : 50

**Section-C :** 04 questions (question may have sub division) covering all units but not more than one question from each unit, descriptive type, answer in about 500 words, 2 questions to be attempted. Total marks : 40

#### **Unit - I**

Kinematics-Lagrangian methods. Equation of Continuity. Boundary surfaces. Stream lines, Path lines and streak lines, Velocity potential, Irrotational and rotational motion. Vortex Lines.

Equations of Motion-Lagrange's and Euler's equations of motion Bernouli's theorem, Equation of motion by flux method.

#### **Unit - II**

Equations referred to moving axes. Impulse reactions. Stream function, Irrotational motion in two-dimensions. Complex velocity potential. Sources. Sinks, Doublets and their images. Conformal mapping. Milne-Thomson circle theorem.

#### **Unit - III**

Two-dimensional Irrotational motion product by motion of circular. co-axial and elliptic cylinders in an infinite mass of liquid. Kinetic energy of liquid. Theorem of Blasius. Motion of a sphere through a liquid at rest at infinity. Liquid streaming past a fixed sphere. Equation of motion of a sphere. Stoke's stream function.

Vortex motion and its elementary properties, Kelvin's proof of permanence. Motions due to circular and rectilinear vortices.

#### **Unit - IV**

Fluid Properties : General properties of Newtonian and Non-newtonian and plastic fluids Stress components in realfluid, Relations between rectangle components of stress. Connection between stresses and gradients of velocity, Navier-stoke equations of motion.

#### **Unit - V**

Plane Poiseuille and Couette flows between two parallel plates. Theory of Lubrication. Flow through tubes of uniform cross section in form of circle, annulus and equilateral triangle under constant pressure gradient, Unsteady flow over a flat plate.

Reynolds number, Prandit's boundary layer. Boundary layer equations in two dimensions. Blasius solution, Boundary layer thickness. Displacement thickness. Karman Integral Conditions. Separation of boundary layer flow.

#### **References :**

1. W.H.Besaint and A.S.Ramsey. Freatiseon Hydromechanics, Part II, CBS Publishers, Delhi 1988.
2. G.K. Batchelor and Introduction to Fluid Mechanics, Foundation, Books, New Delhi 1991.
3. F.Chortion, Textbook of fluid Dynamics, C.B.S, Publishers, Delhi 1985.
4. A.J.Chorin and A.Marsden, A Mathematical Introdution to Fuild Dynamics, Springer-Vertag, New Yark 1993.
5. L.D.Landau and E.M. Lipschitz, Fluid mechanics, Pergamon Press, Londan, 1985.

### **Opt. Paper - III -MATHEMATICAL STATISTICS**

3 Hrs. duration

Max. Marks – 100

**Note :** The question paper will contain three sections as under –

- Section-A :** One compulsory question with 10 parts, having 2 parts from each unit, short answer in 20 words for each part. Total marks : 10
- Section-B :** 10 questions, 2 questions from each unit, 5 questions to be attempted, taking one from each unit, answer approximately in 250 words. Total marks : 50
- Section-C :** 04 questions (question may have sub division) covering all units but not more than one question from each unit, descriptive type, answer in about 500 words, 2 questions to be attempted. Total marks : 40

### Unit - I

Random Variable, Moment Generating Function (MGF) Probability inequalities (Tchebyshef, Markov, Jensen), Convergence in Probability and in distribution, weak law of large numbers and central limit theorem for independent, identically distributed random variable with finite variance, marginal and conditional distribution in multivariate case, Covariance matrix and Correlation Coefficient (Product moment- Partial and multiple), Regression.

### Unit - II

Probability Distributions :- Bernouli, Binomial, Multinomial Hypergeometric, Geometric, Poission Distribution, Probability Distributions : Uniform, Exponential, Cauchy, Gamma, Beta and Normal distribution.

### Unit - III

Sampling Distribution:- t, F, Chi-Square distribution as sampling distribution , Standard errors and large Sampling distribution. Distribution of order statistics and range.

Theory of Statistics:- Methods of estimation, maximum liklihood method, method of moments, minimum chi square method, least square method.

### Unit - IV

Unbiasedness, efficiency, Consistency, Cramer Rao inequality. Statistical Method :- Test of Mean variance in normal distribution one Population and two Population cases, related confidence intervals, Tests of Product Moment, Partial and multiple Corelation Coefficients, Comparision of K. Linear regression, Fitting Polynomial regression, related tests.

### Unit - V

Analysis of discrate data : Chisquare test of goodness of fit, Contingency table Analysis of variance:- one way and two way classification, large sample tests through normal approximation, Non-Parametric tests, Sign test, Median test, rank correlation and test of independence.

### References :

1. Fundamentals of Statistics: Gupta, Kapoor, S.Chand Publications
2. Mathematical Statistics: Kapoor, Saxena, S.Chand Publications

## Opt. Paper - IV -INFORMATION THEORY

3 Hrs. duration

Max. Marks – 100

**Note :** The question paper will contain three sections as under –

- Section-A :** One compulsory question with 10 parts, having 2 parts from each unit, short answer in 20 words for each part. Total marks : 10
- Section-B :** 10 questions, 2 questions from each unit, 5 questions to be attempted, taking one from each unit, answer approximately in 250 words. Total marks : 50
- Section-C :** 04 questions (question may have sub division) covering all units but not more than one question from each unit, descriptive type, answer in about 500 words, 2 questions to be attempted. Total marks : 40

### Unit - I

Basic concepts of probability, Sample spaces, Probability measure, Theorems of addition and multiplication, Conditional probability, Bayes Theorem Random, Variable, Discrete and continuous probability distributions Communication processes.

### Unit - II

Entropy as a measure of uncertainty and information, Shannon's entropy and entropies of order, Algebraic properties and possible interpretations, Analytical properties and inequalities, Joint and conditional entropies, Mutual information.Noiseless coding, Unique decipherability, Conditions of existence of instantaneous codes, Its extension to uniquely decipherable codes, Noiseless coding theorem.

### Unit - III

Construction of optimal codes, Discrete memory less channels, Models for communication channel capacity, Classification of channels, Calculation of channel capacity, Decoding scheme. fundamental theorems, Exponential error bound weak converse of Fundamental theorem.

### Unit - IV

Extension of definition of entropies to continuous memory less channels and properties. Characterization theorem for entropies due to Shannon, Tevberg, Chaundy and Mechleod, Kandall, Daroczy, Campbell and Hayarda- Charvat.

### Unit - V

Error correcting codes- maximum distance, Principal and error correcting properties, Gammings bounds, Paity coding, Upper and Lower bounds of paity cheek codes.

#### Books Recommended :

1. Reza F.M. : Introduction of Information Theory
2. Mathai A.M. and Rathi P.N. : Axiomatic Foundations of some concepts of Information Theory.

## Opt. Paper - V -PROGRAMMING IN C WITH ANSI FEATURES

3 Hrs. duration

Max. Marks – 100

**Note :** The question paper will contain three sections as under –

- Section-A :** One compulsory question with 10 parts, having 2 parts from each unit, short answer in 20 words for each part. Total marks : 10
- Section-B :** 10 questions, 2 questions from each unit, 5 questions to be attempted, taking one from each unit, answer approximately in 250 words. Total marks : 50
- Section-C :** 04 questions (question may have sub division) covering all units but not more than one question from each unit, descriptive type, answer in about 500 words, 2 questions to be attempted. Total marks : 40

### Unit - I

An overview of programming. Programming language, Classification.

C Essentials-Program Development, Functions, Anatomy of a Function, Variables and Constants, Expressions. Assignment Statements. Formatting Source Files. Continuation Character. The preprocessor.

### Unit - II

Scalar Data Types-Declarations, Different Types of Integers. Different kinds of Integer Constants. Floating-Point Types. Initialization. Mixing Types. Explicit Conversions-Casts. Enumeration Type. The Void Data Type. Typedefs. Finding the Address of an object. Pointers.

Control Flow-Conditional Branching. The Switch Statement. Looping. Nested Loops. The break and continue Statements. The goto statement. Infinite Loop.

### Unit - III

Operators and Expressions-Precedence and Associativity, Unary Plus and Minus operators. Binary Arithmetic Operators. Arithmetic Assignment Operators. Increment and Decrement Operators. Comma Operators. Relational Operators. Logical Operators. Bit - Manipulation Operators. Bitwise Assignment Operators. Cast Operator. Size of Operators. Conditional Operator. Memory Operator.

### Unit - IV

Arrays and Pointers-Declaring an Array. Arrays and Memory Initializing Arrays Encryption and Decryption. Pointer Arithmetic. Passing pointers as Function Arguments, Accessing Array. Elements through Pointers. Passing Arrays a Function Arguments. Sorting Algorithms. Strings. Multidimensional Arrays. Arrays of Pointers. Pointers to Pointers. Storage Classes-Fixed vs. Automatic Duration. Scope. Global variables. The register Specific. ANSI rules for the syntax and Semantics of the storage-class keywords. Dynamic Memory Allocation

### Unit - V

Structure and Union-Structures. Linked Lists, Union. enum Declarations. Functions-Passing Arguments. Declarations and Calls, Pointers to Functions. Recursion. The Main Function. Complex Declarations

The C Preprocessor-Macro Substitution. Compilation. Include Facility line Control.

Input and Output-Streams, Buffering. The <stdio.h> Header file. Error Handling. Opening and Closing a file. Reading and writing Data. Selecting an I/O Method, Unbuffered. I/O Random Access. The standard library for Input/Output.

### References :-

1. Peter A.Darnell and Phillip E.Margolis. C: A. Software Engineering Approach, Aarosa Publishing House (Singapur International Student Edition ) 1993.
2. Samiel P. Harkison and Gly L. Steele Jr. C: A Reference manuai 2nd Edition Prentice house 1984
3. Brain n. Kernighan & Dennis M. Ritchie. The C Programme Language, 2nd Edition ANSI 1989

## Opt. Paper-VI-FUNDAMENTALS OF COMPUTER SCIENCE

3 Hrs. duration

Max. Marks – 100

**Note :** The question paper will contain three sections as under –

**Section-A :** One compulsory question with 10 parts, having 2 parts from each unit, short answer in 20 words for each part. Total marks : 10

**Section-B :** 10 questions, 2 questions from each unit, 5 questions to be attempted, taking one from each unit, answer approximately in 250 words. Total marks : 50

**Section-C :** 04 questions (question may have sub division) covering all units but not more than one question from each unit, descriptive type, answer in about 500 words, 2 questions to be attempted. Total marks : 40

### Unit - I

Object Oriented Programming-Classes and Scope, nested classes, pointer class members, Class initialization, assignment and destruction; Overloaded functions and operators.

### Unit - II

Templates including class templates; class inheritance and subtyping, multiple and virtual inheritance.



### Unit - III

Data Structures-Analysis of algorithms,  $q$ ,  $w,0$ ,  $o,w$  notations; Lists. Stacks, and queues: Sequential and linked representations; Trees: Binary tree-search tree implementation, B-tree (concept only).

### Unit - IV

Hashing- open and closed; Sorting : Insertion sort, Shell sort, quick sort, heap sort and their analysis.

### Unit - V

Database System-Role of database systems, database system architecture; Introduction to relation algebra and relational calculus: SQL-basic feature including views: Integrity constraints; Database design-normalization upto BCNF.

Operating Systems-User interface, processor management. I/O management, memory management, concurrency and Security, network and distributed systems.

### References :-

1. S.B. Lipman, J.Lajoi: C++ Primer, Addison Wesley.
2. B. Stroustrup; The C++ Programming Language, Addison wesley.
3. C.J. DATE : Introduction to Database Systems, Addison wesley.
4. C. Ritchie ; Operating Systems-Incorporating UNIX and Windows, BPB Publishers.
5. M.A. Weiss, Data Structures and Algorithm Analysis in C++, Addison wesley

## Opt. Paper - VII-COMPUTER ARCHITECTURE & DATA STRUCTURE

3 Hrs. duration

Max. Marks – 100

**Note :** The question paper will contain three sections as under –

**Section-A :** One compulsory question with 10 parts, having 2 parts from each unit, short answer in 20 words for each part. Total marks : 10

**Section-B :** 10 questions, 2 questions from each unit, 5 questions to be attempted, taking one from each unit, answer approximately in 250 words.

Total marks : 50

**Section-C :** 04 questions (question may have sub division) covering all units but not more than one question from each unit, descriptive type, answer in about 500 words, 2 questions to be attempted. Total marks : 40

### Unit - I

*Computer Architecture :-* Internal Structure and organization of computer. Von Nuemann model and its limitations Taxonomy of Architecture Handles Classification Uniprocessors- Register machines, Stack Machinecs Language directed architectures

### Unit - II

Pipelining Ppelined Arithmetic Units, Example systems, RISC and CISC controversy. Overview of 286, 386,486 and 586 processors. Vector Processors- Vector and array processing, Vectorization, Vector code optimization. Example systems like STAR-100. CYBER-205.

### Unit - III

Multiprocessors- Functional Structures, interconnection networks. Parallel memory organization, System deadlock and protection, multiprocessors Scheduling Algorithms.

Introduction to the concepts of an access data structure and an implementation.

### Unit - IV

Stacks and their C implementation, Infix , Postfix and prefix notations. Recursion is applications and its memory location, Queues, Priority queues and linked lists and their implementation using an array of available nodes as well as dynamic storage.

#### **Unit - V**

Trees-Binary trees, Binary tree representations. The Huffman Algorithm. Representing lists as binary trees. Trees and their applications.

Sorting-General background. Exchange sorts. Selection and tree sorting. Insertion sorts. Merge and Radix sorts.

Internal and external searching. Graphs-A flow problem. Graph traverses are Searching forests.

#### **References :-**

1. H.S. Stone. Jerreduction to Computer Architecture. Galgotia.
2. J.P. Hayes Computer Architecture are organization, McGraw Hill.
3. K.Hwang & Sriggs, computer Architecture, & javaf Processing, McGraw Hill.
4. P.M. Kegge Te Architecture of Process Computers, McGraw Hill.
5. J.L. Hennessy, & D.A. Patterson Computer Architecture : A Quantative Approach. Morgen Kauffmann.
6. J.G. Mayers Advances in Computer Architecture Senn Wiley.
7. Aaron M. Tenessaum, Yedidyah Langea- & Vosnes Augenstein, Data Structure using C, Prentice-Hall of India Pvt. Ltd., New Delhi. 1994.

## **Opt. Paper - VIII - RELATIVITY**

3 Hrs. duration

Max. Marks – 100

**Note :** The question paper will contain three sections as under –

**Section-A :** One compulsory question with 10 parts, having 2 parts from each unit, short answer in 20 words for each part. Total marks : 10

**Section-B :** 10 questions, 2 questions from each unit, 5 questions to be attempted, taking one from each unit, answer approximately in 250 words.

Total marks : 50

**Section-C :** 04 questions (question may have sub division) covering all units but not more than one question from each unit, descriptive type, answer in about 500 words, 2 questions to be attempted. Total marks : 40

#### **Unit - I**

Equation of geodesics for the given metric, Riemann Christoffen tensors and its significance Michelson- Morley experiment, Lorentz-Fitzgerald contraction hypothesis, Postulates of special theory of Relativity, Lorentz transformation.

#### **Unit - II**

Mass, Energy formula, Minkowski's 4 dimensional continuum, Space like and time like intervals.

Hamiltonian principle, Energy - Momentum tensor and its expression for perfect fluid, principle of Covariance, Principle of equivalence.

#### **Unit - III**

Condition for flat space time, Einstein's law of gravitational for empty space and material world, Schwarz child exterior and interior solution for gravitational field.

#### **Unit - IV**

Planetary orbit, three crucial tests, Advances of perihelion, Gravitational deflection of light, Shift in spectral lines, Weyl hypothesis, Displacement of the Fraunhofer lines.

#### **Unit - V**

Einstein and de Sitter models their comparison with the actual universe, Red shift in the spectral line on distant galaxies, Hubble constant, Birkhoff's theorem.

#### **References :**

1. Tolman R.C. : Relativity, Thermodynamics and Cosmology, Oxford University Press.
2. Synge J.L. : Relativity the Special and General North Holland Publishing Company, Amsterdam.
3. Eddington A.S. : The Mathematical Theory of Relativity, Cambridge.

### **Opt. Paper - IX - ASTRONOMY**

Duration – 3 Hrs.

Max. Marks – 100

**Note :** The question paper will contain three sections as under –

**Section-A :** One compulsory question with 10 parts, having 2 parts from each unit, short answer in 20 words for each part. Total marks : 10

**Section-B :** 10 questions, 2 questions from each unit, 5 questions to be attempted, taking one from each unit, answer approximately in 250 words.

Total marks : 50

**Section-C :** 04 questions (question may have sub division) covering all units but not more than one question from each unit, descriptive type, answer in about 500 words, 2 questions to be attempted. Total marks : 40

#### **Unit - I**

Celestial Sphere : Refraction. Meridian Circle, The two body problem : Differential equations and integrals of the problem Reduction to relative co-ordinates. Integration of the two body problem in the plane.

#### **Unit - II**

Time : Heliographic coordinates, Aberration, Parallax, The motion in the orbit, The case of parabolic Orbit Additional consideration, The integrals of the n-body problem, Lagrange's solution of the three body problem, the singularities of the three body problem, The Restricted problem of three bodies, Periodic solution in the neighborhood of the points of liberation .

#### **Unit - III**

Proper motions of stars, definition of proper motions. Relation between proper motions. Tangential velocity and parallax. Radial velocity. The measurement of proper motion. The components of proper motion. The component of proper motion at different epochs referred to the same equation system.

#### **Unit - IV**

The components of proper motion. Secular parallax. The solar motion and radial velocity. The solar in the general case. Statistical parallaxes. Determination of the solar apex from proper motions. Determination of the motion from radial velocities.

#### **Unit - V**

Occultations and Eclipses. Binary star orbitic visual binary, Kowalsky's method of determining the elements of a visual binary orbit. Three masses of stars. Dynamic parallaxes. Spectroscopic binaries. The velocity curve. Method of Lehmann-Filhes, Two spectra visible. The velocity curve, Method of Lehmann-Filhes, Two spectra visible, The mass function. The masses of spectroscopic binaries, Eclipsing binary star.

#### **References :**

1. Smart W.M. : Text Book on Spherical Astronomy.
2. Finlay and Freundlich : Celestial Mechanics.

## **Opt. Paper - X -MATHEMATICAL MODELLING**

Duration – 3 Hrs.

Max. Marks – 100

**Note :** The question paper will contain three sections as under –

**Section-A :** One compulsory question with 10 parts, having 2 parts from each unit, short answer in 20 words for each part. Total marks : 10

**Section-B :** 10 questions, 2 questions from each unit, 5 questions to be attempted, taking one from each unit, answer approximately in 250 words. Total marks : 50

**Section-C :** 04 questions (question may have sub division) covering all units but not more than one question from each unit, descriptive type, answer in about 500 words, 2 questions to be attempted. Total marks : 40

#### **Unit - I**

Techniques, classification and simple illustrations. Mathematical Modelling through ordinary differential equation of first order.

#### **Unit - II**

Mathematical Modelling through systems of ordinary differential equation of first order. Mathematical Modelling through ordinary differential equation of second order.

#### **Unit - III**

Mathematical Modelling through difference equation. Mathematical Modelling through partial differential equations.

#### **Unit - IV**

Mathematical Modelling through graphs. Mathematical Modelling through functional Integral, Delay-differential and differential difference equations.

#### **Unit - V**

Mathematical Modelling through calculus of variations and dynamic programming. Mathematical Modelling through mathematical programming, maximum principle and maximum entropy principle.

#### **Referancies**

1. Mathematical Modelling : J. N. Kapur New Age Int. Pub.
2. Mathematical Modelling : Dr. Maurya Navkar pub. Ajmer

# Optional Paper - XI - HYPERGEOMETRIC FUNCTIONS & POLYNOMIALS

Duration – 3 Hrs.

Max. Marks – 100

**Note :** The question paper will contain three sections as under –

**Section-A :** One compulsory question with 10 parts, having 2 parts from each unit, short answer in 20 words for each part. Total marks : 10

**Section-B :** 10 questions, 2 questions from each unit, 5 questions to be attempted, taking one from each unit, answer approximately in 250 words.

Total marks : 50

**Section-C :** 04 questions (question may have sub division) covering all units but not more than one question from each unit, descriptive type, answer in about 500 words, 2 questions to be attempted. Total marks : 40

## Unit - I

The hypergeometric functions : The Gauss' hypergeometric function  $F(a, c; z)$  its integral form, contiguous function relations, the hypergeometric differential equation, elementary properties, simple and quadratic transformations, Gauss' and Kummer's theorems. **The generalised hypergeometric function  $F(a_1, \dots, a_p; b_1, \dots, b_q; z)$** , its differential equations, contiguous function relations, integral forms, Saalschut's, Whipple's, Dixon's theorems, contour integral representation.

## Unit- II

Bessel function : its differential equation, pure and differential recurrence relations, generating function, modified Bessel function and its properties. **Confluent hypergeometric function  $\phi(a; b; z)$**  : definitions, properties, recurrence relations, Kummer's formulas. **Generating functions**: generating functions of the form  $G(2xt - t^2)$ , sets generated by  $e^t(xt)$  and  $A(t) \exp[-xt / (1-t)]$  and the related theorems.

## Unit- III

**Orthogonal polynomials** : condition for orthogonality, zeros and expansion of polynomials, recurrence relation, the Christoffel - Darboux formula, Bessel's inequality. **Legendre polynomials** : generating functions, differential equations, Rodrigues formula, more generating functions, orthogonality, expansions of  $x^n$ , and analytical functions.

## Unit- IV

**Hermite polynomials** : definition, recurrence relations, Rodrigues formula, integral representation, orthogonality, expansion of polynomials, more generating functions. **Laguerre polynomials** : definitions, recurrence relations, Rodrigues formula, orthogonality, expansion of polynomials and special properties, other generating functions.

## Unit - V

**Jacobi polynomials** : definitions, Bateman's generating function, orthogonality, pure, differential and mixed recurrence relations, Brafman's generating function, expansion in series of polynomials **Ultraspherical and Gegenbauer polynomials** : definition, generating function and related properties.

## Suggested Books :

1. Special functions by E.D. Rainville, Chelsea publishing company, Bronx, New York
2. Special functions by Y.L. Luke, Academic press, New York, London

3. Special functions by M.A. Pathan, P.K. Benarji, V.B.L. Chourasia and MC. Goyal, Ramesh Book Depot, Jaipur
4. Special functions by R.K. Saxena and D.C. Gokharoo, Jaipur Publishing House, Jaipur